



International Max Planck Research School  
for Astronomy and Cosmic Physics at the University of Heidelberg



# Diffusive Shock Acceleration In Radiation Dominated Environments

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# The Problem We Are Addressing

Electron acceleration in environments where



$$U_{ph} \gg \frac{B^2}{8\pi}$$



maximum energy: equilibrium  
between acceleration rate and  
loss rate.

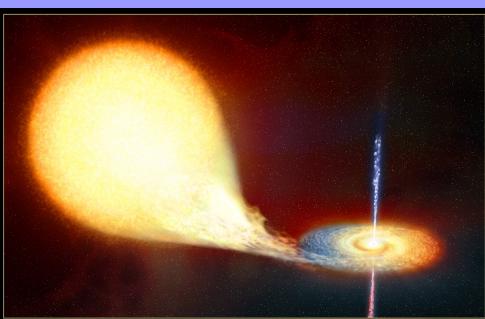
Inverse Compton (IC)  
losses dominant on  
synchrotron.

A situation not yet studied.

Where?

Gamma-ray binaries →

LS 5039 (Cesares et al., 2005)



$$U_{ph} \sim 10 \div 1000 \frac{\text{erg}}{\text{cm}^3} (T \sim 38000 K) \Rightarrow B_{eq} \sim 50 G$$

Galactic Centre (inner 1pc)

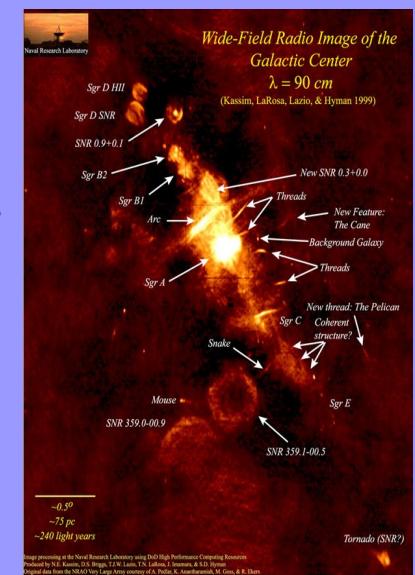
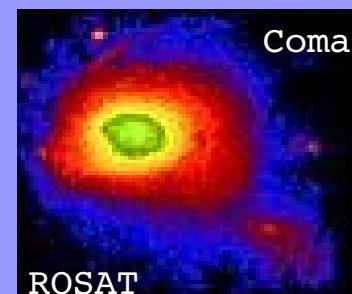
(Davidson et al., 1992)

$$U_{ph} \sim 8 \times 10^{-9} \frac{\text{erg}}{\text{cm}^3} (\text{FIR}[kT = 6 \times 10^{-3} \text{ eV}]) \Rightarrow B_{eq} \sim 500 \mu G$$

Galaxy Clusters

(Carilli & Taylor, 2002)

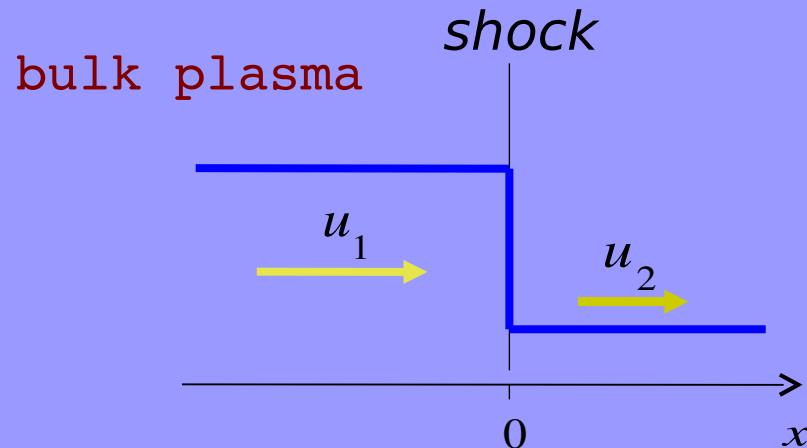
$$U_{ph} \sim 0.25 \frac{\text{eV}}{\text{cm}^3} (T = 2.7 K) \Rightarrow B_{eq} \sim 3 \mu G$$



# The Acceleration

(Fermi, 1949; Bell, 1978)

Diffusive Shock Acceleration:



non thermal particles

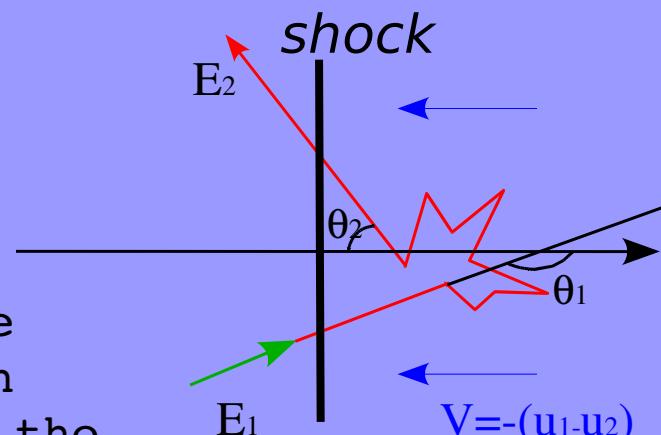
Stochastic acceleration, strong  
non relativistic shocks:

$$\frac{dN}{dE} \propto E^{-2} \Rightarrow f(p) \propto p^{-4}$$

steady state  
distribution  
function at the  
shock position

$$M_1 = \frac{u_1}{c_s} \quad (\text{Mach number})$$

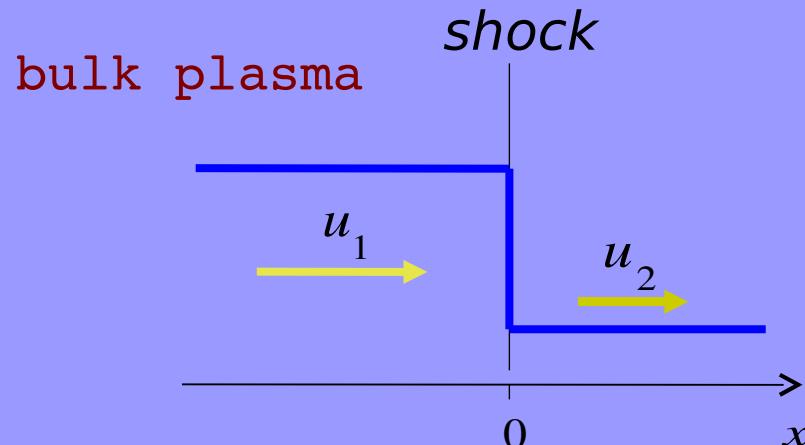
$$R = \frac{u_1}{u_2} \quad (\text{compression ratio})$$



# The Acceleration

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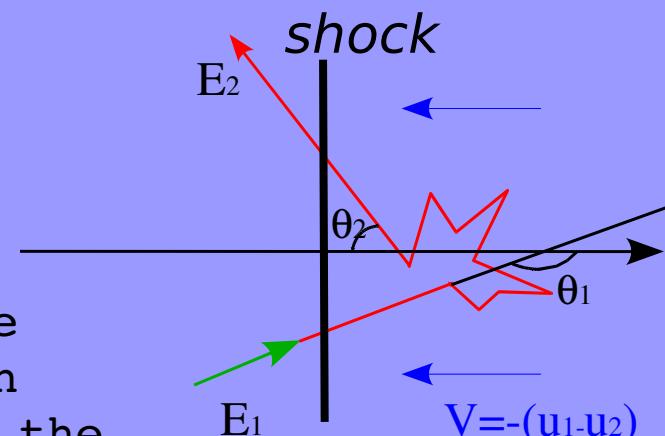
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General approach: assuming the injection spectrum, typically as a power law with exponential cutoff, and introducing losses  $\rightarrow$  photon spectrum.  
Correct solution only if acceleration site and loss site don't coincide.

# The Self-consistent Approach

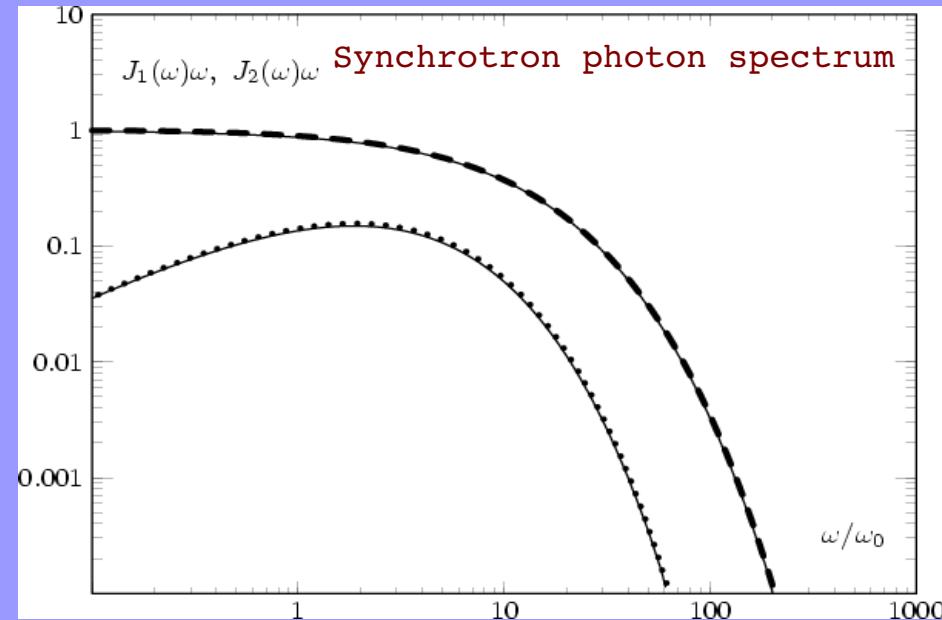
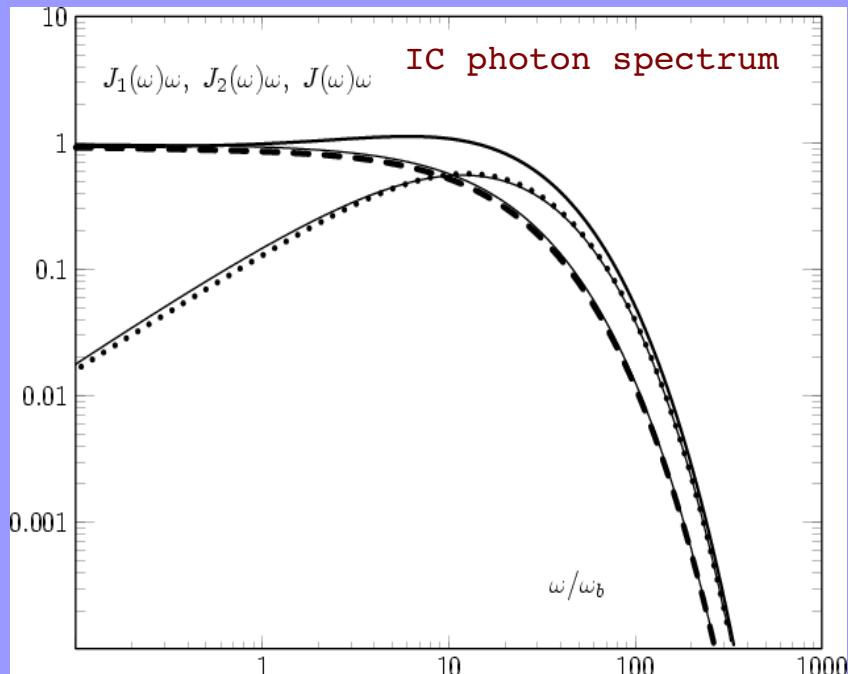
Solving the complete transport equation for electrons:

$$\frac{\partial f(x, p, t)}{\partial t} + u \frac{\partial f(x, p, t)}{\partial x} - \frac{\partial}{\partial x} \left( D \frac{\partial f(x, p, t)}{\partial x} \right) - \frac{p}{3} \frac{\partial u}{\partial x} \frac{\partial f(x, p, t)}{\partial p} + \frac{1}{p^2} \frac{\partial}{\partial p} (p^2 \dot{p} f(x, p, t)) = Q(x, p)$$

loss term

First step: Synchrotron losses  $\propto E^2$

(Webb et al., 1984;  
Heavens & Meisenheimer, 1987;  
Zirakashvili & Aharonian, 2007)



Once obtained  $f(x, p, t) \rightarrow$  IC photon spectrum, under the condition  $U_{ph} \ll \frac{B^2}{8\pi}$ .

# When IC Losses Dominate

IC losses at low energies: Thomson scattering  $\propto E^2$ .

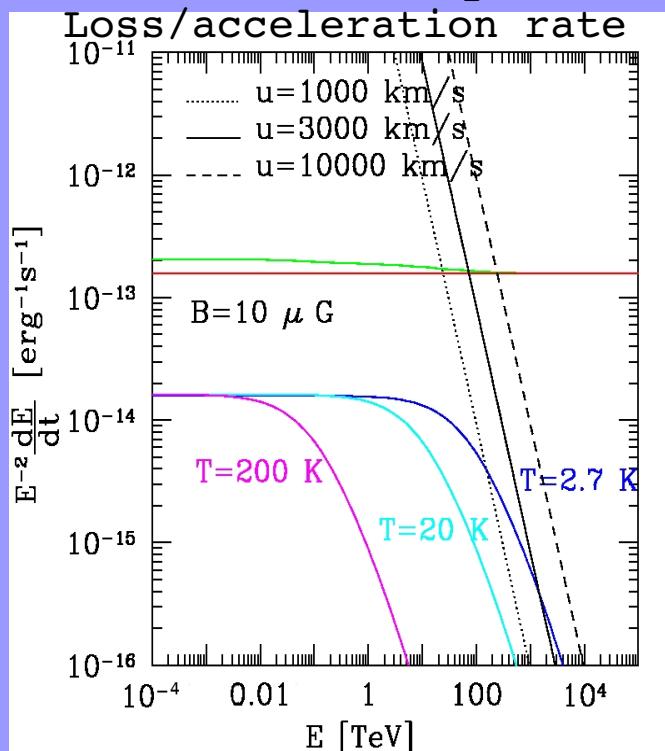
But IC cross section decreases at high energies!

Observed X-ray non-thermal emission in SNR  $\rightarrow$  TeV electrons  
(e.g. Bamba et al., 2003).

Klein-Nishina (KN) regime:  $\frac{\epsilon E_e}{(m_e c^2)^2} > 1$

$$\begin{cases} \text{CMB photons: } E_e \sim 500 \text{ TeV} \\ \text{Optical photons: } E_e \sim 50 \text{ GeV} \end{cases}$$

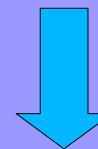
**EXAMPLE:** SN explosion



InterStellar Medium:

(Moskalenko et al., 2006)

$$U_{CMB} \sim 0.25 \frac{eV}{cm^3}; \quad U_{FIR} \sim 0.25 \frac{eV}{cm^3}; \quad U_{OPT/NIR} \sim 0.25 \frac{eV}{cm^3}$$



$$\frac{B^2}{8\pi} \geq U_{ph}$$

Negligible contribution  
of the IC

BUT...

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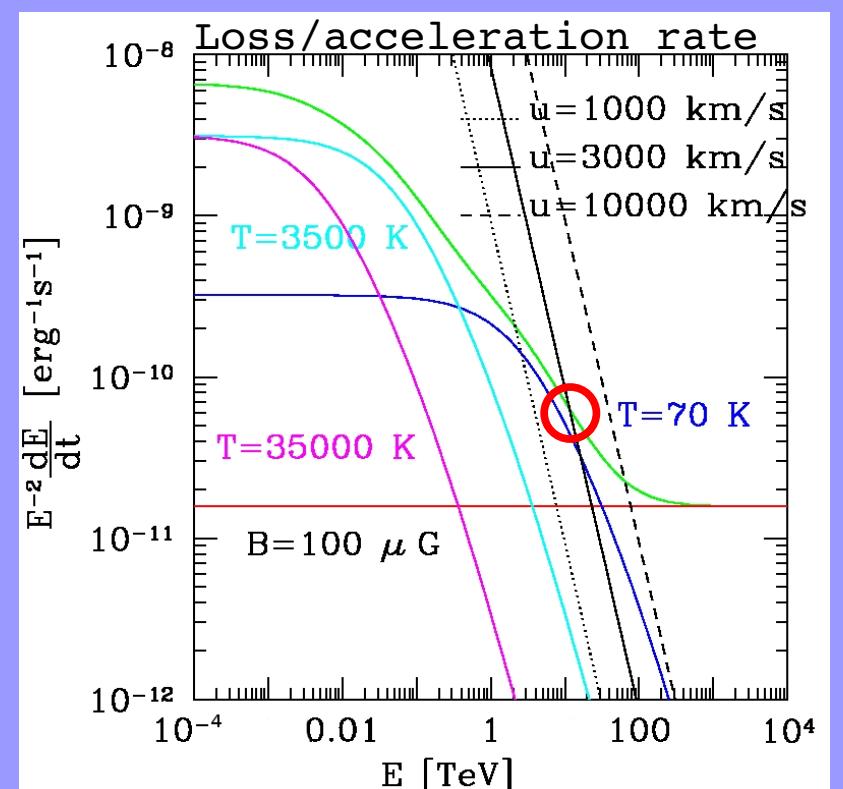
Galactic Centre (inner 1pc):

(Davidson et al., 1992)

$$U_{FIR} \sim 5000 \frac{eV}{cm^3}; U_{NIR} \sim 5 \times 10^4 \frac{eV}{cm^3}; U_{UV/OPT} \sim 5 \times 10^4 \frac{eV}{cm^3};$$

$$B \sim 100 \mu G \quad (\text{Hinton\&Aharonian, 2007})$$

We expect a significant modification of the spectra.



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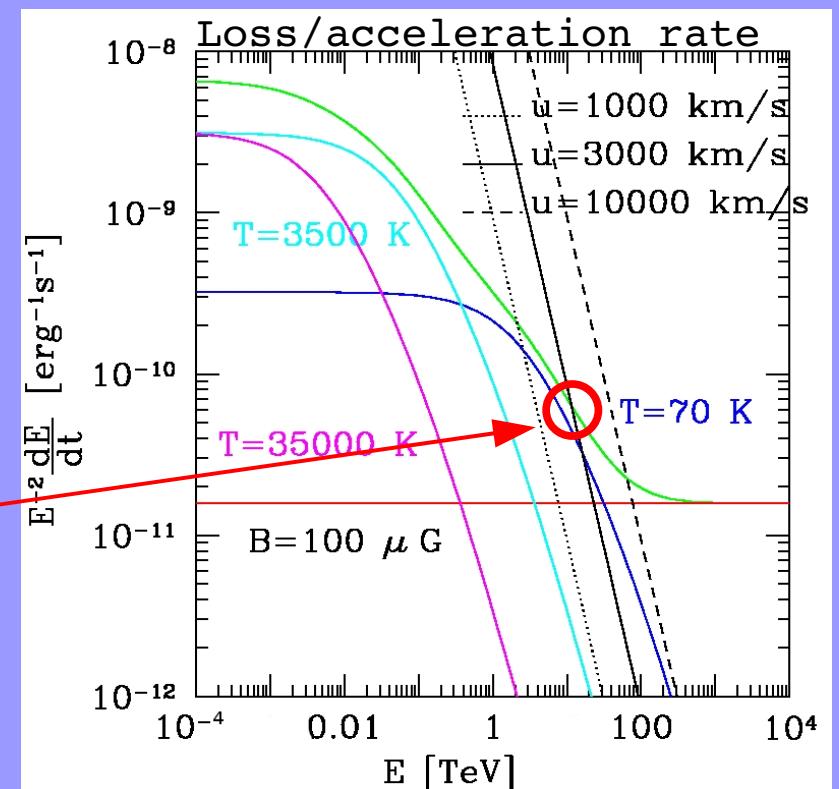
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Depending on  $B$  and  
the shock velocity  $u$   
synchrotron emission  
from soft to hard  
X-rays.

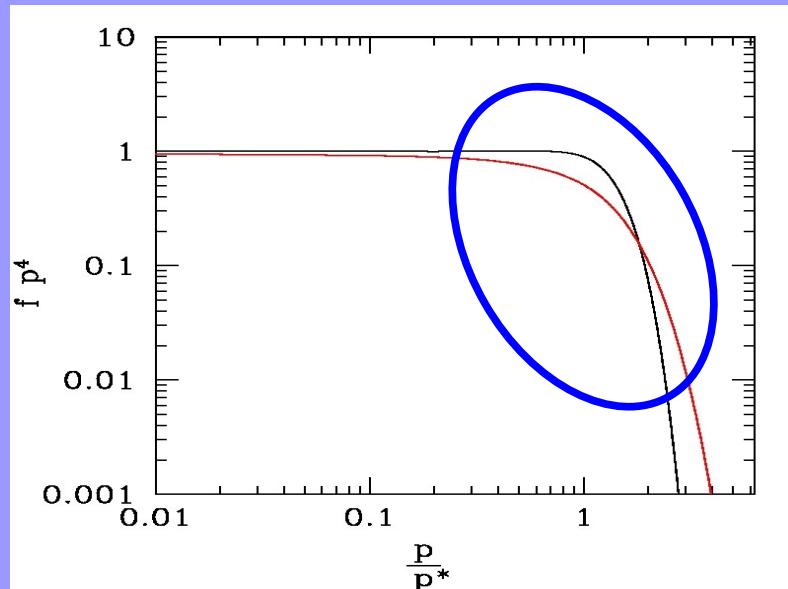
$E^* \sim 10 \text{ TeV}$   
 $\epsilon_\gamma \sim 1 \text{ keV}$



# Results: The Electron Spectrum

(Vannoni, Gabici&Aharonian, to be submitted)

One realistic case: SNR in the inner Galactic Centre.



Electron spectrum at the shock surface (arbitrary normalization).

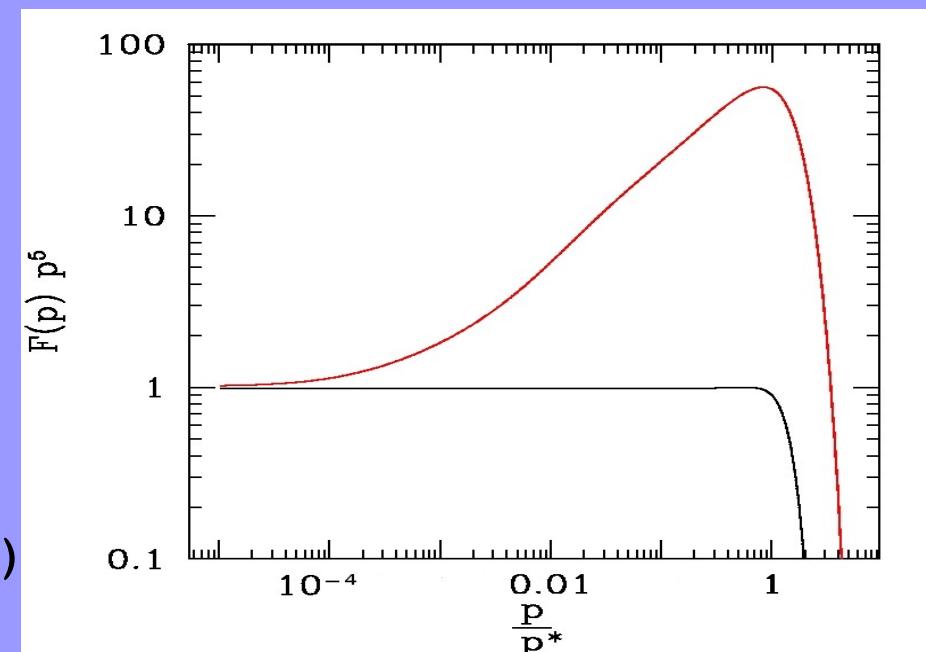
In the IC (KN) loss dominated regime (red curve):

- broader cutoff region
- shallower cutoff shape

Electron spectrum integrated over the up + down-stream regions.

Hardening due to the KN effect, pile up around the cutoff energy up to a factor  $\sim 100$  compared to pure synchrotron losses.

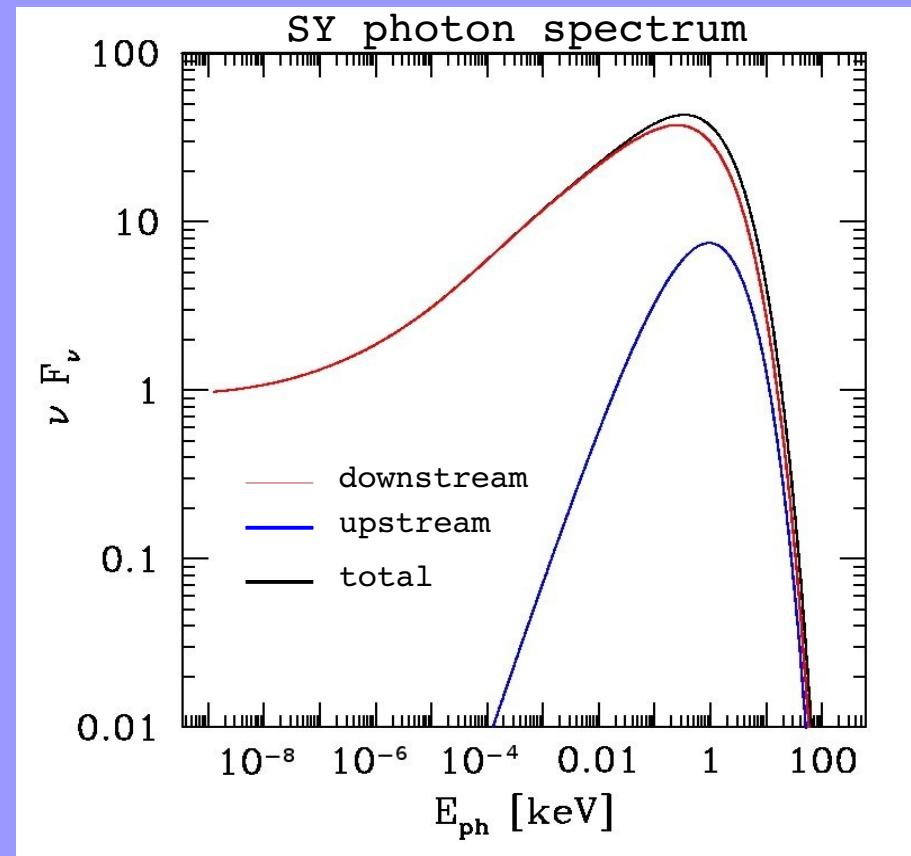
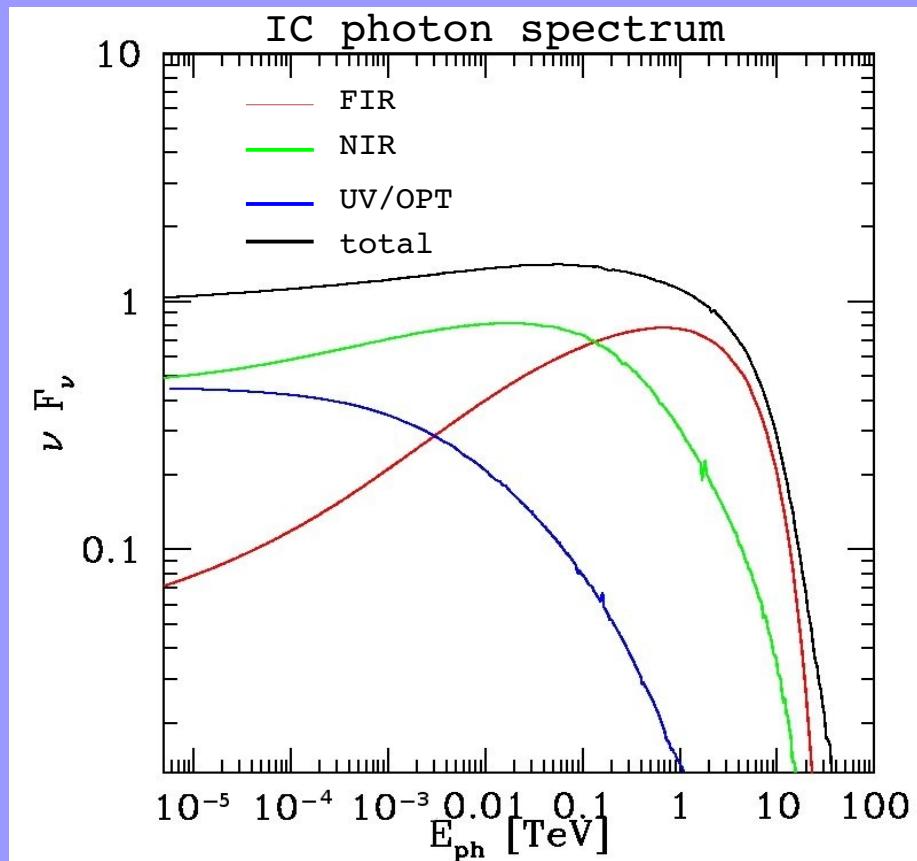
(watch out for the normalization!)



# Results: The Photon Spectrum

(Vannoni, Gabici&Aharonian, to be submitted)

Change in the electron spectrum → features in the photon spectra.



KN cross-section modifies both  
the electron and the photon  
spectrum in opposite directions.

Almost perfect compensation

The bump in the electron  
distribution is reproduced in  
the synchrotron spectrum.

Pile up at keV energies

# Outlook

- ◆ Electron accelerators embedded in a strong radiation field: IC can become the dominant loss channel.
- ◆ Klein-Nishina effects can set in, significantly affecting the particle spectrum (pile up at the cutoff).
- ◆ Impact on the radiation (Synchrotron and IC).
  - ➡ Most significant feature in the synchrotron spectrum.

## Specific sources (work in progress):

SNR in the Galactic Centre: (depending on values of B and shock velocity)

electrons cutoff energy  
~1÷100 TeV

synchrotron pile up in the UV/X-rays  
~few eV÷100 keV

## More (still to explore):

Microquasar: multi keV synchrotron from electrons in the jet  
(may require relativistic DSA).

Galaxy Clusters: if IC on the CMB is the dominant channel  
we expect features in keV synchrotron photons.

